


Academic Year: 2015 – 2016 Semester: Summer Date: August 2016	 Modern University for Technology & Information مستقبل الصفوة Faculty of Pharmacy	Mathematics: OCM 103 Final Exam Duration Time: 2 Hours																
Answer All Questions		No. of questions: 4 Total Mark: 60																
Question 1																		
(a) If $A = \begin{bmatrix} 0 & 3 & -2 \\ 2 & 1 & -1 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 1 & 0 \\ 0 & 3 & 4 \end{bmatrix}$ Find, if possible, $A + B$, $A.A$, $A.B$, $A.A^t$, $ A $, $ A^t.B $.	6																	
(b) Find the eigenvalues and eigenvectors of : $A = \begin{bmatrix} 0 & 1 \\ 3 & 2 \end{bmatrix}$.	5																	
(c) Solve the linear system : $x + y = 3$, $2x - 3y = 1$, $3x - 2y = 4$	5																	
Question 2																		
(a) Find y' where:	12																	
(i) $y = 2x^4 + 4^x + x$	(ii) $y = 3 + x^3 \cdot \ln x$	(iii) $y = \cos 4x \cdot \log x$																
(iv) $y = [2x - \sin x]^4$	(v) $y = \cos x + \cos^4 x$	(vi) $y = \frac{2}{x^2} + \frac{\ln x}{x}$																
(b) Find the integrals:	12																	
(i) $\int (x^{-4} + 4^x) dx$	(ii) $\int (\frac{2}{3x} + \frac{1}{x^3}) dx$	(iii) $\int (\cos x - \sin x) dx$																
(iv) $\int (\sqrt{x} + e^x) dx$	(v) $\int x \cos x dx$	(vi) $\int_0^1 (3 + x^2)^2 dx$																
Question 3																		
(a) Find the extrema of the function : $f(x) = x^4 - 2x^2 + 1$	5																	
(b) If a drug exists in three dosage forms : The first of concentration 1 mg / tablet , The second of concentration 2 mg / tablet , The third of concentration 4 mg /tablet. If the pharmacist wanted to produce 8 tablets of concentration 2.5 mg / tablet by mixing whole tablets. Find two possible solutions.	5																	
Question 4																		
(a) If y is the quantity of drug decreases according to the equation $\frac{dy}{dt} = -\frac{1}{y}$. Find y as function of the time t where the initial quantity is 4 units. Also, find (i) The value of y after 2 hours. (ii) The time at which there is no drug in the blood.	5																	
(b) If the quantity of a drug in the blood decreases according to the data:	5																	
<table><tr><td>Time: t</td><td>0</td><td>2</td><td>4</td><td>6</td><td>8</td><td>10</td><td>Hours</td></tr><tr><td>Quantity: y</td><td>12</td><td>11</td><td>9</td><td>6</td><td>2</td><td>1</td><td>Units</td></tr></table>	Time: t	0	2	4	6	8	10	Hours	Quantity: y	12	11	9	6	2	1	Units		
Time: t	0	2	4	6	8	10	Hours											
Quantity: y	12	11	9	6	2	1	Units											
From these data, find the relation $y = a + bt$.																		

Good Luck

Dr. Mohamed Eid